

## ARITHMATIC PROGRESSION

**MATHEMATICS** 

**10TH ICSE** 

- 1. Given below is the group-wise heights of children in cms in a sports academy:
  - i. Group A: 131, 141, 115, 161
  - ii. Group B: 119, 125, 131, 137
  - iii. Group C: 102, 130, 142, 150
  - iv. Group D: 105, 104,103, 101

Which of the above groups forms an AP?

- 2. Determine k so that 4k + 8,  $2k^2 + 3k + 6$ ,  $3k^2 + 4k + 4$  are the three consecutive terms of an A.P.
- 3. Write the first four terms of the AP whose first term a and common difference d are given as follows:
  - i. a = 4, d = 6
  - ii. a = 10, d = -3
- 4. Find the 16<sup>th</sup> term of the AP: 3, 10, 17, 24...
- 5. Which term of the AP : 2, 7, 12, 17 is 67 ?
- 6. The 7<sup>th</sup> term of an AP is -4 and its 13 th term is -16. Find the A.P.
- 7. Check whether -83 is a term of the AP 5,2, -1, -4.....
- 8. How many two- digit numbers are divisible by 6?
- 9. Find the 12<sup>th</sup> term from the last term (towards the first term) of the AP: 21, 18, 15,..., -81.
- 10. For what value of n, the nth terms of two AP's, 63,65,67... and 3, 10,17,... are equal?
- 11. If 5 times the 5<sup>th</sup> term of an AP is equal to 10 times the 10<sup>th</sup> term, show that its 15<sup>th</sup> term is zero.
- 12. Find the middle term of AP, 6, 1 3,20,...., 216.
- 13. Which term of the AP: 120 116, 112,.... is its first negative term?
- 14. If the pth, qth and rth term of an AP are x, y and z respectively, then show that x(1 r) + y(r p) + z(p q) = 0.
- 15. Find the sum of the first 20 terms of the A.P. 3,15,27, 39,...
- 16. If the sum of the first 22 terms of an AP is 979 and its first term is 8, find its  $10^{th}$  term.
- 17. How many terms of the AP 9, 17, 2 5,... must be taken to give a sum of 636?
- 18. Find the sum of the first 25 terms of an A.P. where nth term is given by  $a_n = 2 3n$ .
- 19. The sum of the first n terms of an A.P. is  $3n^2 + 4n$ . Find the 25th term of this A.P.
- 20. The sum of the first 8 terms of an A.P. is 100 and the sum of its firs 19 terms is 551. Find the first term and the common difference of the A.P.
- 21. Find the sum of integers between 100 and 200 that are (i) divisible by 6 (ii) not divisible by 6.
- 22. Find the middle term of the sequence formed by all- digit numbers which leave remainder 3, when divided by 4. Also find the sum of all numbers on both sides of the middle term separately.
- 23. Nidhi saves Rs.2 on the first day of a month, Rs.4 on the second day, Rs.6 on the third day and so on. What will be her saving in the month of February if it is a leap year?

PERL EDUCATION - 1st Floor, Shrinath Complex, Sahakar Nagar Chowk, Aurangabad MH - 431001 Contact: 0240-2950011, 8767256768

- 24. The sum of the first n terms of three A.P.'s are  $S_p S_2$  and  $S_3$ . The first term of each is 5 and their common differences are 2,4 and 6 respectively. Prove that  $S_1 + S_3 = 2S_2$ .
- 25. The ratio of the sum of the first m and n terms of an A.P. is  $m^2 : n^2$ . Show that the r atio of its mth and nth terms is (2m 1) : (2n 1).
- 26. A sum of Rs.700 is to be used to give seven cash prizes to students of a school for their overall academic performance, If each prize is Rs.20 less than its preceding prize, find the value of each of the prizes.
- 27. Determine whether the given sequence is geometric or not. If it is, find the common ratio.
  - i. -1, 6, -36, 216,...
  - ii. 4,16, 36,64,....
- 28. Find the nth term of the G.P. -3, -15, -75, -375,... and hence its 7<sup>th</sup> term.
- 29. If the nth term of a G.P. is  $2 \times \left(\frac{1}{4}\right)^{n-1}$ , find the first five terms of the G.P.
- 30. Which the term of the sequence 6, 2,  $\frac{2}{3}$ , ... is  $\frac{2}{243}$ .
- 31. Find the G.P. whose fourth term is 24 and seventh term is 192.
- 32. Find the first term and the number of terms in a G.P. if the fourth, seventh and last terms are 10, 80, and 2560 respectively?
- 33. If the pth, qth and rth terms of a G.P. are x, y, and z respectively, prove that  $x^{q-r}$ .  $y^{r-p}$ .  $z^{p-q} = 1$ .
- 34. Find the sum of the G.P. 4,2, 1 ... to 10 terms.
- 35. How many terms of the G.P. 5, 20, 80 ... must be taken to make the sum 6825?
- 36. If the third term of a G.P. is  $\frac{5}{2}$  and its eight term is  $\frac{5}{64}$ , then find the sum of its first 10 terms.
- 37. In a G.P., the ratio of the sum of the first three terms to that of first six terms is 125 : 152. Find the common ration of the G.P.

PERL EDUCATION - 1st Floor, Shrinath Complex, Sahakar Nagar Chowk, Aurangabad MH - 431001 Contact: 0240-2950011, 8767256768

#### PERL EDUCATION



# ARITHMETIC PROGRESSION

# **MATHEMATICS**

### **10TH ICSE**

- 1. Is the Sequence 12, 8, 4, 0, ..... an A.P? If yes; state its first term and common difference.
- 2. For the A.P. 7, 15, 23, 31, ...., write the first term, common difference and text two terms.
- 3. Find the A.P. whose  $n^{th}$  term is 2n 3.
- 4. Find the  $n^{th}$  term and the 20<sup>th</sup> term of the sequence : 9, 5, 1, -3, .....
- 5. Is 205 a term of the sequence 8, 12, 16, 20, .....?
- 6. Find the A.P. whose second term is 12 and 7<sup>th</sup> term exceeds the 4<sup>th</sup> by 15.
- 7. Find the A.P. whose  $6^{\text{th}}$  term = 5 and  $10^{\text{th}}$  term = 9.
- 8. Which term of A.P. 4·2, 4·7, 5·2, 5·7, ....., is 8·7?
- 9. Find the 12<sup>th</sup> term from the end in A.P. 13, 18, 23, ....., 158.
- If 8 times the eighth term of an A.P. is equal to 15 times its fifteenth term, find its 23<sup>th</sup> term.
- 11. Find the number of all natural numbers between 20 and 80, which are divisible by 3.
- 12. How many whole numbers, each divisible by 7, lie between 200 and 500?
- 13. Which term of the A.P. 4, 11, 18, 25, ..... is 42 more than its 25<sup>th</sup> term ?
- 14. Find the sum of the first 20 terms of the A.P. : 5, 8, 11, 14, ......
- 15. Find the sum of first ten terms of the A.P. : 8, 4, 0, -4, -8, ......
- 16. Find the sum of the first 40 terms of the A.P. whose 4<sup>th</sup> term is 8 and 6<sup>th</sup> term is 14.
- 17. For the A.P. : 10, 15, 20, ....., 195; find :
  - i. The number of terms in the above A.P.
  - ii. The sum of all its terms.
- 18. Find the sum of first 16 terms of a sequence whose  $n^{th}$  term is given by  $t_n = 5n 3$ , where n is a natural number.
- 19. How many terms of the A.P. 43, 39, 35, ..... be taken so that their sum is 252 ?
- 20. How many terms of the A.P. 20,  $19\frac{1}{3}$ ,  $18\frac{2}{3}$ , ..... must be taken so that their sum is 300 ?
- 21. The sum of three terms in A.P. is 33 and their product is 1155. Find the terms.
- 22. If a, b and c are in A.P., show that : (b + c), (c + a) and (a + b) are also in A.P.

PERL EDUCATION - 1st Floor, Shrinath Complex, Sahakar Nagar Chowk, Aurangabad MH - 431001 Contact: 0240-2950011, 8767256768 23. A sum of 2 8,000 is invested at 10% simple interest per annum. Calculate the interest at the end of each year.

Does the Sequence of interests at the end of consecutive years form an A.P. ? If yes, write its first term and the common difference.

24. In a school, students stand in rows. If 30 students stand in the first row, twenty-seven in the second row, twenty four in the third row and six in the last row; find how many rows are there and what is the total number of students ?

