

RATIONAL AND IRRATIONAL NUMBER

MATHEMATICS **DPP-1**

CLASS-9th ICSE

1. Find a rational number between $\frac{1}{5}$ and $\frac{7}{10}$

- 2. Give three rational numbers lying between $\frac{1}{3}$ and $\frac{1}{2}$.
- 3. Find four rational numbers between $\frac{1}{4}$ and $\frac{1}{3}$.
- 4. Find 7 rational numbers between $\frac{1}{3}$ and $\frac{1}{3}$.
- Find three rational numbers lying between $\frac{-2}{5}$ and $\frac{-1}{5}$
- Find 10 rational numbers between $\frac{-2}{5}$ and $\frac{1}{2}$.
- 7. Express each decimal as a fraction in simplest for,.
 - i. 0.8
 - ii. 1. 27
 - iii. $0.\overline{407}$
- 8. Convert (i) $0.\overline{47}$, (ii) $4.23\overline{48}$ into fractions in the simplest form.
- 9. Express the following in the form of $\frac{p}{q}$, where p and q are integers and $1 \neq 0$.
- 10. Find the value of $2.\overline{6} 0.\overline{9}$.
- 11. Explain $0.6 + 0.\overline{7} + 0.4\overline{7}$ in the form of $\frac{p}{q}$, where p and q are integers and $q \neq 0$.
- 12. Examine whether $\sqrt{2}$ is rational or irrational. (b) show that $\sqrt{2}$ is not a rational number.
- 13. Show that $\sqrt{3}$ is not a rational number.
- 14. Identify the following as rational or irrational.

i.
$$\sqrt{9}$$

ii.
$$5\sqrt{12}$$

iii.
$$\sqrt{1.96}$$

iv.
$$\sqrt{\frac{6}{18}}$$

v.
$$-\sqrt{0.81}$$

vi.
$$\sqrt{625}$$

vii.
$$(\sqrt{2} - 3)^2$$

viii.
$$(\sqrt{7} +) (\sqrt{7} - 1)$$

ix.
$$(\sqrt{2} + \sqrt{3})(\sqrt{7} + \sqrt{5})$$

$$\mathbf{X.} \qquad \frac{14}{2\sqrt{7}}$$

15. State with reason which of the following are surds and which are not:

i.
$$\sqrt{98}$$

ii.
$$\sqrt{7} \times \sqrt{28}$$

iii.
$$\sqrt[3]{2} \times \sqrt[3]{32}$$

- $15\sqrt{20} \div 4\sqrt{45}$
- $20\sqrt{7} \div 15\sqrt{21}$

16. Rationalise the denominator of

i.
$$\frac{1}{\sqrt{7}}$$

ii.
$$\frac{1}{5\sqrt{3}}$$

iii.
$$\frac{1}{\sqrt[3]{4}}$$

- 17. Rationalise the denominator and simplify:

i.
$$\frac{26}{\sqrt{13}}$$

ii.
$$\frac{3}{\sqrt{27}}$$

- iii.
- iv.
- 18. Rationalise the denominators of the following:

i.
$$\frac{1}{2-\sqrt{3}}$$

ii.
$$\frac{2}{\sqrt{3}-\sqrt{2}}$$

iii.
$$\frac{1}{\sqrt{2} + \sqrt{3}}$$

iii.
$$\frac{1}{\sqrt{2} + \sqrt{3}}$$

iv.
$$\frac{\sqrt{x} - 3}{\sqrt{x} + 3}, x \ge 0$$

v.
$$\frac{2\sqrt{3}+6\sqrt{7}}{\sqrt{2}-\sqrt{3}}$$
 vii. $\frac{y^2}{\sqrt{y^2+y^2+4}}$ vi. $\frac{5-3\sqrt{2}}{5+3\sqrt{2}}$

- 19. Rationalise the denominator and simplify $\frac{3\sqrt{2}}{\sqrt{3}+\sqrt{6}} \frac{4\sqrt{3}}{\sqrt{6}+\sqrt{2}} + \frac{\sqrt{6}}{\sqrt{2}+\sqrt{3}}$.
- 20. Find the values of a and b if $\frac{\sqrt{3}-1}{\sqrt{3}+1} = a + b \sqrt{3}$. 21. Rationalise the denominator of $\frac{1}{\sqrt{2}+\sqrt{3}+\sqrt{10}}$

PERL EDUCATION DPP

RATIONAL AND IRRATIONAL NUMBERS

CLASS - IX ICSE MATHEMATICS

DPP - 2

1.	Which of the rational numbers $\frac{3}{5}$ and $\frac{5}{7}$ is greater. Insert three rational numbers between	$\frac{3}{5}$ and
	$\frac{5}{7}$ so that all the five numbers are in ascending order of their values.	

2. Without doing any actual division, find whether each of the following is a terminating decimal or not;

i.
$$\frac{17}{50}$$

ii. $\frac{7}{8}$

iii. $\frac{23}{72}$

3. Show that $\sqrt{2}$ is an irrational number.

4. Prove that $\sqrt{5} - \sqrt{3}$ is irrational.

5. Prove that $\sqrt{8} + 5$ is irrational.

6. Identify each of the following as rational or irrational number.

i.
$$\sqrt{12}$$

ii.
$$3\sqrt{2} \times \sqrt{8}$$

7. Insert a rational number and an irrational number between 3 and 4

8. Find two irrational numbers between 2 and 3

9. Examine each of the following as a rational or an irrational number

i.
$$(3+\sqrt{2})^2$$

ii.
$$(3+\sqrt{3})(3-\sqrt{3})$$

iii.
$$\frac{6}{\sqrt{3}}$$

10. Insert two rational number and two irrational numbers between $\sqrt{3}$ and $\sqrt{7}$

11. Which of the following numbers is grater:

i.
$$3\sqrt{2}$$
 and $2\sqrt{3}$

ii.
$$6\sqrt[3]{3}$$
 and $5\sqrt[3]{4}$

12. Compare:

i.
$$\sqrt[3]{4}$$
 and $\sqrt{3}$

ii.
$$\sqrt[4]{8}$$
 and $5\sqrt[6]{22}$

13. State, with reasons, which of the following is a surd and which is not:

i.
$$\sqrt{27}$$

ii.
$$\sqrt{225} \times \sqrt{4}$$

14. Find the least rationalizing factor of:

i.
$$\sqrt{27}$$
,

ii.
$$2\sqrt{125}$$

15. Rationalize the denominator of

i.
$$\frac{1}{\sqrt{2}}$$

ii.
$$\frac{5}{2\sqrt{2}}$$

16. Simplify each of the following by rationalizing the denominator:

i.
$$\frac{1}{3-\sqrt{7}}$$

ii.
$$\frac{3}{\sqrt{5}+\sqrt{3}}$$

iii.
$$\frac{\sqrt{3}-\sqrt{2}}{\sqrt{3}+\sqrt{2}}$$

iv.
$$\frac{7}{\sqrt{15}+2\sqrt{2}}$$

V.
$$\frac{30}{5\sqrt{3}-3\sqrt{5}}$$

17. Find the values of 'a' and 'b' " $\frac{2\sqrt{3}-3\sqrt{2}}{2\sqrt{3}-3\sqrt{2}} = a + b\sqrt{6}$.

18. If $x=2+\sqrt{3}$, find the value of $x^2+\frac{1}{x^2}$

19. Prove that $\frac{1}{\sqrt{2}+1} + \frac{1}{\sqrt{3}+\sqrt{2}} + \frac{1}{2+\sqrt{3}} = 1$

20. Rationalize the denominator of : $\frac{1}{\sqrt{3}+\sqrt{2}-1}$

21. Evaluate:

$$\frac{1}{3-\sqrt{8}} - \frac{1}{\sqrt{8}-\sqrt{7}} + \frac{1}{\sqrt{7}-\sqrt{6}} - \frac{1}{\sqrt{6}-\sqrt{5}} + \frac{1}{\sqrt{5-2}}$$

22. If $\sqrt{3} = 1.73$, find the value of : $\frac{2+\sqrt{3}}{2-\sqrt{3}} + \frac{2-\sqrt{3}}{2+\sqrt{3}} + \frac{\sqrt{3}-1}{\sqrt{3}+1} - \frac{\sqrt{3}+1}{\sqrt{3}-1}$

23. If $x=3+2\sqrt{3}$, check whether $x+\frac{1}{x}$ is rational or irrational.