MATHEMATICS ICSE - 9

PERL Education



1. State giving reasons, whether the two given triangles are congruent or not



- **2.** A St. line AB is bisected at C and through C a St. line DC is drawn perpendicular to AB. Prove that AD=BD.
- **3.** AX is the bisector of \angle BAC; P is any point on AX. Prove that the perpendiculars drawn from P to AB and AC are equal.
- 4. In fig. it is given that AC= BD and AC=BC. Prove that $\triangle ABD \cong \triangle ABC$.



- **5.** If $\triangle ABC$ is an isosceles triangles such that AB=AC, then altitude AD from A on BC bisects BC.
- 6. In a \triangle ABC, the internal bisectors of \angle B and \angle C meet at O. Prove that OA is the internal bisector of \angle A.
- 7. In the figure two sides AB and BC and the median AD drawn to one of these sides of the △ABC are equal to the two sides PQ and QR and the corresponding median PM of the other △PQR. Prove that the two triangles are congruent.



PERL EDUCATION - 1st Floor, Shrinath Complex, Sahakar Nagar Chowk, Aurangabad MH - 431001 Contact : 0240-2950011, 87672 56768

PERL Education

8. In figure, explain how one can find the breadth of the river without crossing it.



9. Shyam wishes to determine the distance between two objects A and B but there is an obstacle between the two objects (as shown in the fig.) which prevents him from making a direct measurement. He designs an ingenious way to overcome this difficulty. First, he fixes a pole at convenient point O so that from O, both ends are visible. Then he fixes another pole at a point D on the line AO (produced) such that AO=DO. In a similar way, he fixes a third pole at a point C on the BO (produced) such that BO = CO. then the measures CD and finds that CD= 170 cm. prove that the distance between the objects A and B is also 170 cm.

- 10. A point O is taken inside a rhombus ABCD such that its distances from the angular points D and B are equal. Show that AO and OC are in one and the same st. line.
 In △ABC, ∠A =40° and AB = AC. Find ∠B and ∠C.
- **11.** Find the lettered angles from the following figures.



12. Prove that each angle of an equilateral triangle is 60°

PERL EDUCATION - 1st Floor, Shrinath Complex, Sahakar Nagar Chowk, Aurangabad MH - 431001 Contact : 0240-2950011, 87672 56768 **13.** In figure it is given that LM=MN, QM=MR, ML \perp PQ and MN \perp PR. Prove that PQ=PR.



14. AD, BE and CF, the altitudes of \triangle ABC are equal. Prove that \triangle ABC is an equilateral triangle. **15.** In figure it is given that AB= BC and AD =EC. Prove that \triangle ABE $\cong \triangle$ CBD.



- **16.** In a right angled triangle, one acute angle is double the other, prove that the hypotenuse is double the smallest side.
- **17.** If in $\triangle ABC$, BC = CA and $\angle A = 35^\circ$, which is the longer. BC or AB?
- **18.** PQRS is a quadrilateral with PS as its greatest and QR as its least side, Prove that $\angle PQR \ge \angle PSR$ and $\angle QRS \ge \angle SPQ$.
- **19.** Prove that the hypotenuse is the greatest side in a right- angled triangle.
- **20.** If S is any point on the base QR produced, of an isosceles $\triangle PQR$, prove that PS>PQ
- **21.** Show that the sum of the three altitudes of a triangle is less than the sum of the three sides of the triangle
- **22.** (a)Prove that any two sides of a triangle are together greater than twice the median drawn to the third side.
 - (b) Hence, prove that the perimeter of a triangle is greater than the sum of its medians.
- **23.** In the given figure, $PS \perp 1$ and SR>SQ. Prove that PR>PQ.

